

## TITLE OF THE INVENTION

### IMAGE ALIAS REJECTION USING SHAPED STATISTICAL FILTERING

## BACKGROUND OF THE INVENTION

5           The present invention relates to video processing, and more particularly to a method of image alias rejection using shaped statistical filtering in a waveform rasterizer.

10           There is a well-known problem in waveform rasterization that, when rasterizing a high resolution waveform onto a limited resolution display, an artifact appears that is sometimes called "jaggies". There are existing "de-jaggie" algorithms for line drawing, such as that described in U.S. Patent No. 4,586,037 by Harvey J. Rosener et al issued April 29, 1986 and entitled "Raster Display Smooth Line Generation", but with video waveforms generally are not lines. The jaggies seen in a rasterized waveform, which is a bit-map display, may be understood as the spatial aliases of an undersampled image. 15 If the waveform is originally rasterized in a much higher resolution, such as 2048x2048, then is subjected to an appropriate spatial low pass filter which "smears" the points over several neighboring pixels of the raster, and then is subsampled to the desired display resolution, such as 640x480, this removes 20 the jaggies. However for this approach the high resolution image needs a very large raster memory. This memory also needs to be very fast due to the needs of waveform rasterization.

          Rasterization works by building up an image of plotted x-y values. Each new x-y data point, where x may represent time and y may represent 25 amplitude, adds to the image which is then scanned out in a raster fashion for

further processing and/or display. In an ideal rasterizer a new data point may be plotted anywhere in the image without regard to where a previous data point was plotted. One way to deal with the need for low pass filtering is to subject each new input data point to a spatial low pass filter and then plot the outputs of the spatial filter in the desired display resolution memory.

However if a 2x2 spatial kernel is used, which is the smallest practical, four memory cycles are needed to plot the output of the spatial filter. Memory bandwidth is often the limiting item in rasterization, so doing four times as many memory cycles is not what is desired.

What is desired is image alias rejection that minimizes the number of display memory cycles.

#### BRIEF SUMMARY OF THE INVENTION

Accordingly the present invention provides a method of image alias rejection using shaped statistical filtering in a waveform rasterizer which eliminates the need for a high resolution memory and does not use multiplication. High resolution "X" and "Y" data are each combined with a dither value from a shaped random number generator. The combined "X" and "Y" values are then truncated as appropriate for a lower resolution display and stored in a display raster memory.

The objects, advantages and other novel features of the present invention are apparent from the following detailed description when read in conjunction with the appended claims and attached drawing.

## BRIEF DESCRIPTION OF THE SEVERAL VIEWS OF THE DRAWING

Fig. 1 are representations (a) of a traditional filter kernel and (b) of a statistical filter kernel with corresponding results.

Fig. 2 is a block diagram view of an apparatus for image alias rejection according to the present invention.

Fig. 3 is a simple schematic view of the apparatus of Fig. 2 according to the present invention.

Fig. 4 are plan views of a waveform display (a) without image alias rejection and (b) with image alias rejection according to the present invention.

## DETAILED DESCRIPTION OF THE INVENTION

The present invention addresses the image alias rejection problem by filtering with a shaped statistical filter. A simple one-dimensional example is shown in Fig. 1. For a traditional filter implementing a low pass filter for spreading an impulse over several bins, the impulse is passed through a kernel (Fig. 1a) with coefficients of  $1/4$ ,  $1/2$  and  $1/4$  in this example. The coefficients are multiplied by the impulse to provide an output. On the other hand a statistical filter has a random shaped function representing a probability density function for the impulse response of the filter being implemented. In this example (Fig. 1b) the statistical filter puts whatever input is provided in the first bin one-fourth of the time, in the second bin one-half of the time and in the third bin one-fourth of the time. If the impulse is put into the statistical filter many, many times, as is common for portions of a video signal such as sync, color burst, test patterns, etc., the output is

approximately the same as for the traditional filter. This is useful in rasterization since the image is made up of many data point plots.

The statistical filter places each data point into a single bin based on the probability density function of the filter. Over time the ensemble response of the filter resembles a traditional filter with an impulse response matching the probability density function of the statistical filter. Examples range from a uniform probability density function corresponding to a rectangular impulse response generated by a single random number generator, to a Gaussian random number generator producing an equivalent gaussian impulse response. This gaussian random number generator may be implemented using the central limit theorem by summing the outputs of several independent and identically distributed random number generators, as shown in Fig. 2-10, page 31 of "The Scientist and Engineer's Guide to Digital Signal Processing" by Steven W. Smith and published (Second Edition 1999) by California Technical Publishing ([www.DSPguide.com](http://www.DSPguide.com)).

Referring now to Fig. 2 the "X" and "Y" data for a waveform sample from respective sources **12, 14** are combined in respective summing circuits **16, 18** at high precision, such as 12 bits, with the dither outputs of respective shaped random number generators **20, 22**, where the shape is a function of the number of individual shaped random number generators being summed to provide the dither outputs. The resulting sums are "subsampling" by respective truncation elements **24, 26**, such as to 9 or 10 bits depending upon the subsampling required, and stored in a display raster memory as part of a display plotting system **28**.

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The shaped random number generator **20** may be formed by at least two linear feedback shift registers **40<sub>1</sub> . . . 40<sub>n</sub>** clocked by the input clock and enabled by an RNG enable signal. The outputs from the linear feedback shift registers **40** are input to a second summation circuit **42**, the output of which is a dither signal according to the desired statistical shape function. An RNG register **44** stores the dither signal each cycle of the input clock. Although this implementation uses multiple linear feedback shift registers **40** to form the shaped random number generator **20**, the linear feedback shift registers may be replaced with a comparable look-up table.

The dither signal from the RNG register **44** is input to a summation circuit **50** together with the sweep value from the sweep register **36**, and then stored in an output register **52** as the filtered "X" value prior to truncation.

Referring now to Fig. 4 a typical video waveform is shown (a) without and (b) with image alias rejection as described above. The aliased waveform shows uneven or discontinuous characteristics especially along the vertical portions, while the waveform with image alias rejection shows a smooth characteristic comparable to an analog display.

Thus the present invention provides image alias rejection using a statistical filter for a rasterized waveform image by taking the "X" and/or "Y" data point values and combining them with a dither signal from a shaped random number generator, the result being subsampled or truncated to a desired lower resolution for display.